Politechnika Wrocławska

## Fundamentals of engineering drawing

dr inż. Stanisław Frąckowiak

## Parallel orthogonal projection according to Monge's method

Let's assume:
x and y horizontal projection plane $\pi 1$ $x$ and $z$ vertical projection plane $\pi 2$ $y$ and $z$ side projection plane $\pi 3$


## Parallel orthogonal projection according to Monge's method

The projecting rays form parallel beams that pass through the points $\mathrm{A}, \mathrm{B}, \mathrm{C} \ldots$ and pierce successively the projection planes $\pi 1, \pi 2, \pi 3$ $\pi 1$ - projection direction k1 || to the z -axis (') $\pi 2$ - projection direction k2 || to y -axis (") $\pi 3$ - projection direction k3 || to the x-axis ("')


## Parallel orthogonal projection according to Monge's method

Each pair of planes among m1, m2, m3 intersect at right angles along the axes, called projection axes:

$$
\begin{aligned}
& \pi_{1} \cap \pi_{2} \rightarrow x \\
& \pi_{1} \cap \pi_{3} \rightarrow y \\
& \pi_{2} \cap \pi_{3} \rightarrow z
\end{aligned}
$$

## Parallel orthogonal projection according to Monge's method

- The planes $\pi 1, \pi 2, \pi 3$ divide space into eight areas
- Let's stick to area „!"



## Parallel orthogonal projection according to Monge's method

Monge's method consists in projecting the elements of space onto three mutually perpendicular projection planes, assuming a perpendicular projection direction



## Parallel orthogonal projection according to Monge's method

The plane of the drawing as a result of unifying viewports is a plane $\boldsymbol{\Pi}_{\mathbf{2}}$

## The image of a point in Monge projections

Guiding the projecting rays:
$A A^{\prime}=h$, height of point $A$ relative to $\pi 1$
$A A^{\prime \prime}=\mathrm{g}$, depth of point A relative to $\pi 2$
$A A ">=s$, width of point A relative to $m 3$


## The image of a point in Monge projections

- We consider the dimensional number of the height ( h ) to be positive when the point is located above the horizontal viewport
- We consider the depth dimensional number ( g ) to be positive when the point is in front of the vertical viewport


## Specific point locations



height $\mathrm{h}=0$
Point A lies on m1
depth $\mathrm{g}=0$
Point A lies on $\pi 2$

width $\mathrm{s}=0$
Point A lies on $\pi 3$

## The image of a straight line in Monge projections

- We choose two points $A$ and $B$ in space that uniquely determine the line a.
- The projections of these points determine the projections of the line a



## The image of a straight line in Monge projections

## - Line a and in any position



Axonometry (dimetry)


Parallel orthogonal projection (Monge method)

## Plane in Monge projections

- The plane in space is determined by the basic elements:
- 3 points not on one straight line ( $\mathrm{A}, \mathrm{B}, \mathrm{C}$ )
- line and a point not on this line ( $a, A$ )
- two intersecting lines (a, b)
- two parallel lines (a, b)


## Traces of lines and planes

- In Monge's projections, due to the clarity of information transfer, we present lines and planes in the form of traces.
- Traces are points of projection plane piercing (through a line or a plane)


## Traces of line

- trace of the horizontal straight line (a') - piercing point $\pi 1=\mathrm{Ha}$
- trace of the straight line (a") - piercing point $\pi 2=\mathrm{Va}$
- trace of a straight line (a'") - piercing point $\pi 2=K a$



## Construction of traces of a straight line in a particular position

- the line a' intersects the $x$-axis as the horizontal projection of m 2 at the point Va ( (the horizontal projection of the vertical trace)



## Improper items

- Cases when:
- straight lines are parallel
- the planes are parallel
- the line and the plane are parallel



## Improper items

- Then we are talking about improper elements not taken into account by Euclidean geometry, and introduced by projective geometry.
- Inappropriate elements were introduced for the purposes of descriptive geometry to enable the preservation of spatial problem solving schemes
- We assume that mutually parallel elements are "almost parallel", i.e. that they intersect at a point that is infinitely far away
- line a" intersects the x -axis as the vertical projection of the viewport m1 at the improper point $\mathrm{Ha}{ }^{\circ} \infty$
- The point $\mathrm{Ha}{ }^{\infty} \infty$ lies "infinitely far" on the direction of line a", will intersect the horizontal projection of line a (a') at the point "infinitely far" Ha' ${ }^{\prime}=$ Наळ




## Example

- $\mathrm{H}_{\mathrm{a}}, \mathrm{V}_{\mathrm{a}}=$ ?



## Example - view in axonometry



## Example

- $\mathrm{H}_{\mathrm{a}}, \mathrm{V}_{\mathrm{a}}=$ ?




## Example

- $\mathrm{H}_{\mathrm{a}}, \mathrm{V}_{\mathrm{a}}=$ ?


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## Traces of the plane

- Let's take three points $X, Y, Z$ defining an arbitrary plane on the axes $x, y, z$ of the reference system. The pairs of points $X$ and $Y, X$ and $Z, Y$ and $Z$ belong simultaneously to the plane $a$ and subsequent projection planes - thus determining the traces of the plane a in the proj. planes



## Traces of the plane

- horizontal trace of the plane - straight line - intersection of the planes a and $\pi 1=h a$
- vertical trace of the plane - straight line - common part of the plane $\alpha$ and $\pi 2=v a$
- trace of the plane - straight line - common part of the plane a and $\pi 3=k a$


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## Determination of traces of a plane defined by points and lines

- "If the line a belongs to the plane a defined by traces, then the traces of this line (points) lie on the corresponding traces of the plane (lines),,
- Knowing the traces of lines belonging to the plane a, we can unambiguously determine the traces of this plane

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## Example

$$
\mathbf{h}_{\alpha}, \mathbf{v}_{\alpha}=?
$$



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## Example

$$
\mathbf{h}_{\alpha}, \mathbf{v}_{\alpha}=?
$$

## Associated elements

- Common edge (intersection) of two planes ( $\alpha \cap B=k$ )
- Piercing point of a straight line ( $a \cap a=P$ )


## Common edge of two planes

- The horizontal traces ha and hB of the planes intersect at the point Hk
- The vertical traces va and vB of the planes intersect at the point Vk



## Common edge of two planes

- The points Hk and Vk determine the intersection of the planes - the (straight) edge $\mathbf{k}$ given by projections $\mathbf{k}^{\prime}$ and $\mathbf{k}^{\prime \prime}$



## Common edge of two planes

To specify edge k in projections:

- define the horizontal and vertical projection of the Hk point (horizontal trace of the intersection edge)
- define the horizontal and vertical projection of the point Vk (vertical trace of the intersection edge)


## Example

$k^{\prime}, k^{\prime \prime}=$ ?


## Example

$$
k^{\prime \prime}
$$

$k^{\prime}, k^{\prime \prime}=$ ?


## Example

$k^{\prime}, k^{\prime \prime}=$ ?


## Example



## Piercing point of a straight line through a plane

- Piercing point ( $\mathrm{a} \cap \mathrm{a}=\mathrm{P}$ )



## Piercing point of a straight line through a plane

The procedure for searching for the piercing point of a straight line: we determine the auxiliary plane $\varepsilon$ passing through the line a we find the edge (k) common to the planes a and $\varepsilon$ ( $\mathrm{a} \cap \varepsilon=\mathrm{k}$ )


Since line a lies on plane $\varepsilon$ and line $k$ lies on plane, so these lines will intersect at point $P$, which is the intersection point of plane a


## Example



## Example

$\mathbf{P}^{\prime}, \mathbf{P}{ }^{\prime}=$ ?


## Homework

2/1

- Find traces of line $a, H a, V a=$ ?
- Find traces of plane $\alpha, h_{\alpha}, v_{\alpha}=$ ?

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- Find intersection between planes $\alpha$ and $\beta$
- Find piercing point of plane $\alpha$ by line a

